Pyglmnet: Python implementation of elastic-net regularized generalized linear models

Mainak Jas$^{1, 2}$, Titipat Achakulvisut$^3$, Aid Idrizović$^4$, Daniel Acuna$^5$, Matthew Antalek$^6$, Vinicius Marques$^4$, Tommy Odland$^7$, Ravi Prakash Garg$^6$, Mayank Agrawal$^8$, Yu Umegaki$^9$, Peter Foley$^{10}$, Hugo Fernandes$^{11}$, Drew Harris$^{12}$, Beibin Li$^{13}$, Olivier Pieters$^{14, 20}$, Scott Otterson$^{15}$, Giovanni De Toni$^{16}$, Chris Rodgers$^{17}$, Eva Dyer$^{18}$, Matti Hamalainen$^{1, 2}$, Konrad Kording$^3$, and Pavan Ramkumar$^{19}$

1 Massachusetts General Hospital 2 Harvard Medical School 3 University of Pennsylvania 4 Loyola University 5 University of Syracuse 6 Northwestern University 7 Sonat Consulting 8 Princeton University 9 NTT DATA Mathematical Systems Inc 10 605 11 Rockets of Awesome 12 Epoch Capital 13 University of Washington 14 IDLab-AIRO – Ghent University – imec 15 Clean Power Research 16 University of Trento 17 Columbia University 18 Georgia Tech 19 System1 Biosciences Inc 20 Research Institute for Agriculture, Fisheries and Food

Summary

Generalized linear models (GLMs) are well-established tools for regression and classification and are widely applied across the sciences, economics, business, and finance. Owing to their convex loss, they are easy and efficient to fit. Moreover, they are relatively easy to interpret because of their well-defined noise distributions and point-wise nonlinearities.

Mathematically, a GLM is estimated as follows:

$$\min_{\beta_0, \beta} \frac{1}{N} \sum_{i=1}^{N} L(y_i, \beta_0 + \beta^T x_i) + \lambda P(\beta)$$

where $L(y_i, \beta_0 + \beta^T x_i)$ is the negative log-likelihood of an observation $(x_i, y_i)$, and $\lambda P(\cdot)$ is the penalty that regularizes the solution, with $\lambda$ being a hyperparameter that controls the amount of regularization.

Modern datasets can contain a number of predictor variables, and data analysis is often exploratory. To avoid overfitting of the data under these circumstances, it is critically important to regularize the model. Regularization works by adding penalty terms that penalize the model parameters in a variety of ways. It can be used to incorporate our prior knowledge about the parameters’ distribution in a structured form.

Despite the attractiveness and importance of regularized GLMs, the available tools in the Python data science eco-system do not serve all common functionalities. Specifically:

- **statsmodels** provides a wide range of noise distributions but no regularization.
- **scikit-learn** provides elastic net regularization but only limited noise distribution options.
- **lightning** provides elastic net and group lasso regularization, but only for linear (Gaussian) and logistic (binomial) regression.
Pyglmnet is a response to a fragmented ecosystem

Pyglmnet offers the ability to combine different types of regularization with different GLM noise distributions. In particular, it implements a broader form of elastic net regularization that include generalized L2 and L1 penalties (Tikhonov regularization and Group Lasso, respectively) with Gaussian, Binomial, Poisson, Probit, and Gamma distributions. The table below compares pyglmnet with existing libraries as of release version 1.1.

<table>
<thead>
<tr>
<th>Distributions</th>
<th>pyglmnet</th>
<th>scikit-learn</th>
<th>statsmodels</th>
<th>lightning</th>
<th>py-glm</th>
<th>Matlab</th>
<th>glmnet in R</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gaussian</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
</tr>
<tr>
<td>Binomial</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
</tr>
<tr>
<td>Poisson</td>
<td>x</td>
<td>x</td>
<td></td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>x</td>
</tr>
<tr>
<td>Poisson (softplus)</td>
<td>x</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Probit</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gamma</td>
<td>x</td>
<td></td>
<td>x</td>
<td></td>
<td></td>
<td></td>
<td>x</td>
</tr>
</tbody>
</table>

Pyglmnet is an extensible pure Python implementation

Pyglmnet implements the algorithm described in Friedman, J., Hastie, T., & Tibshirani, R. (2010) and its accompanying popular R package glmnet. As opposed to python-glmnet or glmnet_python, which are wrappers around this R package, pyglmnet is written in pure Python for Python 3.5+. Therefore, it is easier to extend and more compatible with the existing data science ecosystem.

Pyglmnet is unit-tested and documented with examples

Pyglmnet has already been used in published work (Benjamin et al., 2017; Bertrán et al., 2018; Höfling, Berens, & Zeck, 2019; Rybakken, Baas, & Dunn, 2019). It contains unit tests and includes documentation in the form of tutorials, docstrings and examples that are run through continuous integration.

Example Usage

Here, we apply pyglmnet to predict incidence of violent crime from the Community and Crime dataset, one of 400+ datasets curated by the UC Irvine Machine Learning Repository (Dua & Graff, 2019) which provides a highly curated set of 128 demographic attributes of US counties. The target variable (violent crime per capita) is normalized to the range of [0, 1]. Below, we demonstrate the usage of a pyglmnet’s binomial-distributed GLM with elastic net regularization.
from sklearn.model_selection import train_test_split
from pyglmnet import GLMCV, simulate_glm, datasets

# Read dataset and split it into train/test
X, y = datasets.fetch_community_crime_data()
Xtrain, Xtest, ytrain, ytest = train_test_split(X, y, test_size=0.33)

# Instantiate a binomial-distributed GLM with elastic net regularization
glm = GLMCV(distr='binomial', alpha=0.05, score_metric='pseudo_R2', cv=3, tol=1e-4)

# Fit the model and then predict
glm.fit(Xtrain, ytrain)
yhat = glm.predict_proba(Xtest)

As illustrated above, pyglmnet’s API is designed to be compatible with scikit-learn (Buitinck et al., 2013). Thus, it is possible to use standard idioms such as:

```python
glm.fit(X, y)
glm.predict(X)
```

Owing to this compatibility, tools from the scikit-learn ecosystem for building pipelines, applying cross-validation, and performing grid search over hyperparameters can also be employed with pyglmnet’s estimators.

Acknowledgements

Pyglmnet development is partly supported by NIH NINDS R01-NS104585 and the Special Research Fund (B.O.F.) of Ghent University.

References


