

Bayesian X-ray Analysis (BXA) v4.0

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Summary

BXA connects the X-ray spectral analysis environments Xspec ([Arnaud, 1996](#)) and Sherpa ([Freeman et al., 2001](#)) with modern Bayesian inference algorithms based on nested sampling. This allows estimation of parameter probability distributions and model comparison with Bayes factors. Because BXA is a plug-in, users can build and fit the full range of models available in Xspec and Sherpa. BXA also comes with convenience functionality for backgrounds of many X-ray missions, which allow extracting more information from low-count data.

Statement of need

In X-ray spectroscopy, the instrument responses are often not trivial, which means that forward folding is required to test models against data. Judging realistic physical models, which can be degenerate, against data, which sometimes consist of few photon counts, is a challenge. Bayesian inference provides a good solution in this setting.

For parameter estimation, Bayesian inference updates an initial state of information using the data and a model into a new state (posterior probability distribution). In practice, Bayesian inference algorithms approximate the posterior by Monte Carlo sampling. Before BXA, Bayesian X-ray spectral analyses have been implemented with Markov Chain Monte Carlo (MCMC). The variants include Metropolis random walks (e.g., [van Dyk et al., 2001](#)) and affine-invariant ensembles ([Goodman & Weare, 2010](#)). These can be difficult to initialise and/or tune, and require complicated checks of the chain convergence to determine when to terminate the computation, and how to select good posterior samples from the chain. The MCMC variants have limitations when models have multiple posterior peaks. These are common in the additive models typically considered in X-ray astronomy when combined with data sets of low spectral quality. For these reasons, Bayesian X-ray analyses, as implemented in existing popular packages, can be unsatisfying.

BXA uses nested sampling ([Skilling, 2004](#)) to efficiently generate posterior samples. Nested sampling performs a global scan of the parameter space, without requiring a user-defined starting point. This makes it robust and easy to use in large X-ray surveys with many objects, and in situations where many models should be compared. Nested sampling can be substantially more efficient than MCMC in low-dimensional settings ($d < 10$) ([Speagle, 2020](#)).

Comparing astrophysical models is currently primarily performed either using likelihood ratio tests (F-test) or Monte Carlo simulations to evaluate goodness-of-fit measures. The former are often invalid ([Protassov et al., 2002](#)), while the latter are computationally very expensive. Bayesian model comparison with posterior odds ratios, provides an alternative approach, which is natural in Bayesian inference. BXA (via nested sampling) makes Bayesian model comparison

computationally feasible to apply and calibrate with simulated data (see e.g., [J. Buchner et al., 2014](#)).

Features

BXA connects the X-ray spectral analysis environments Xspec/Sherpa to the nested sampling algorithm UltraNest for Bayesian parameter estimation and model comparison.

BXA provides the following features:

- parameter estimation in arbitrary dimensions, which involves:
 - finding the best fit
 - computing error bars
 - computing marginal probability distributions
 - parallelisation with MPI
- plotting of spectral model vs. the data:
 - for the best fit
 - for each of the solutions (posterior samples)
 - for each component
- model selection:
 - computing the Bayesian evidence for the considered model, ready for use in Bayes factors
 - unlike likelihood-ratios, not limited to nested and linear models
- model discovery:
 - visualize deviations between model and data with binning-independent Quantile-Quantile (QQ) plots.
- empirical background models:
 - for getting more information out of low-count spectra

BXA shines especially

- when systematically analysing a large data-set, or
- when comparing multiple models
- when analysing low counts data-set with realistic models

because its robust and unsupervised fitting algorithm explores even complicated parameter spaces in an automated fashion. The user does not need to initialise to good starting points. The algorithm automatically runs until convergence, and slows down to sample carefully if complicated parameter spaces are encountered. This allows building automated analysis pipelines.

Methods

The methods and limitations of BXA were presented in more detail in ([J. Buchner et al., 2014](#)). Until v3.0, BXA employed the Fortran package MultiNest ([Feroz et al., 2009](#)) to perform Bayesian inference. Since v4.0, BXA uses the Python package UltraNest ([Johannes Buchner, 2018](#)), which is easier to install.

For diagnosing the quality of BXA outputs, verifying the stability over two or more runs is recommended, in particular of the marginal posterior distributions and excess scatter of $\log Z$ (Higson et al., 2019).

To determine reliable model selection thresholds, parametric bootstrap is recommended. This involves simulating many data sets under one model and deriving Bayes factor distributions with BXA runs (e.g., Appendix of J. Buchner et al., 2014).

Documentation

[Extensive documentation](#) is available.

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Early versions of BXA for Sherpa were based on pybloccs code ([CHASC Astro-Statistics Collaboration, 2011](#)).

References

- Arnaud, K. A. (1996). XSPEC: The First Ten Years. In G. H. Jacoby & J. Barnes (Eds.), *Astronomical data analysis software and systems v* (Vol. 101, p. 17). http://adsabs.harvard.edu/cgi-bin/nph-data_query?bibcode=1996ASPC..101...17A&link_type=ARTICLE&db_key=AST&high=
- Buchner, Johannes. (2018). UltraNest. In *GitHub repository*. GitHub. <https://github.com/JohannesBuchner/UltraNest>
- Buchner, J., Georgakakis, A., Nandra, K., Hsu, L., Rangel, C., Brightman, M., Merloni, A., Salvato, M., Donley, J., & Kocevski, D. (2014). X-ray spectral modelling of the AGN obscuring region in the CDFS: Bayesian model selection and catalogue. *564*, A125. <https://doi.org/10.1051/0004-6361/201322971>
- CHASC Astro-Statistics Collaboration. (2011). pybloccs. In *GitHub repository*. GitHub. <https://github.com/brefsdal/pybloccs>
- Feroz, F., Hobson, M. P., & Bridges, M. (2009). MULTINEST: an efficient and robust Bayesian inference tool for cosmology and particle physics. *398*, 1601–1614. <https://doi.org/10.1111/j.1365-2966.2009.14548.x>
- Freeman, P., Doe, S., & Siemiginowska, A. (2001). Sherpa: a mission-independent data analysis application. In J.-L. Starck & F. D. Murtagh (Eds.), *Society of photo-optical instrumentation engineers (SPIE) conference series* (Vol. 4477, pp. 76–87). <https://doi.org/10.1117/12.447161>
- Goodman, J., & Weare, J. (2010). Ensemble samplers with affine invariance. *Communications in Applied Mathematics and Computational Science*, Vol. 5, No. 1, p. 65–80, 2010, 5, 65–80. <https://doi.org/10.2140/camcos.2010.5.65>

- Higson, E., Handley, W., Hobson, M., & Lasenby, A. (2019). NESTCHECK: diagnostic tests for nested sampling calculations. *483*(2), 2044–2056. <https://doi.org/10.1093/mnras/sty3090>
- Protassov, R., van Dyk, D. A., Connors, A., Kashyap, V. L., & Siemiginowska, A. (2002). Statistics, Handle with Care: Detecting Multiple Model Components with the Likelihood Ratio Test. *571*, 545–559. <https://doi.org/10.1086/339856>
- Skilling, J. (2004). Nested sampling. *AIP Conference Proceedings*, *735*(1), 395. <https://doi.org/10.1063/1.1835238>
- Speagle, J. S. (2020). DYNESTY: a dynamic nested sampling package for estimating Bayesian posteriors and evidences. *493*(3), 3132–3158. <https://doi.org/10.1093/mnras/staa278>
- van Dyk, D. A., Connors, A., Kashyap, V. L., & Siemiginowska, A. (2001). Analysis of Energy Spectra with Low Photon Counts via Bayesian Posterior Simulation. *548*, 224–243. <https://doi.org/10.1086/318656>