

exoplanet: Gradient-based probabilistic inference for exoplanet data & other astronomical time series

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DOI: [10.21105/joss.03285](https://doi.org/10.21105/joss.03285)

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Submitted: 04 May 2021

Published: 22 June 2021

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Summary

exoplanet is a toolkit for probabilistic modeling of astronomical time series data, with a focus on observations of exoplanets, using PyMC3 ([Salvatier et al., 2016](#)). PyMC3 is a flexible and high-performance model building language and inference engine that scales well to problems with a large number of parameters. exoplanet extends PyMC3's modeling language to support many of the custom functions and probability distributions required when fitting exoplanet datasets or other astronomical time series.

While it has been used for other applications, such as the study of stellar variability (e.g., [Gillen et al., 2020](#); [Medina et al., 2020](#)), the primary purpose of exoplanet is the characterization of exoplanets (e.g., [Gilbert et al., 2020](#); [Plavchan et al., 2020](#)) or multiple star systems (e.g., [Czekala et al., 2021](#)) using time series photometry, astrometry, and/or radial velocity. In particular, the typical use case would be to use one or more of these datasets to place constraints on the physical and orbital parameters of the system, such as planet mass or orbital period, while simultaneously taking into account the effects of stellar variability.

Statement of need

Time domain astronomy is a priority of the observational astronomical community, with huge survey datasets currently available and more forthcoming. Within this research domain, there

is significant investment into the discovery and characterization of exoplanets, planets orbiting stars other than our Sun. These datasets are large (on the scale of hundreds of thousands of observations per star from space-based observatories such as *Kepler* and *TESS*), and the research questions are becoming more ambitious (in terms of both the computational cost of the physical models and the flexibility of these models). The packages in the *exoplanet* ecosystem are designed to enable rigorous probabilistic inference with these large datasets and high-dimensional models by providing a high-performance and well-tested infrastructure for integrating these models with modern modeling frameworks such as PyMC3. Since its initial release at the end of 2018, *exoplanet* has been widely used, with 64 citations of the Zenodo record (Foreman-Mackey et al., 2021) so far.

The *exoplanet* software ecosystem

Besides the primary *exoplanet* package, the *exoplanet* ecosystem of projects includes several other libraries. This paper describes, and is the primary reference for, this full suite of packages. The following provides a short description of each library within this ecosystem and discusses how they are related.

- *exoplanet*¹ is the primary library, and it includes implementations of many special functions required for exoplanet data analysis. These include the spherical geometry for computing orbits, some exoplanet-specific distributions for eccentricity (Kipping, 2013a; Van Eylen et al., 2019) and limb darkening (Kipping, 2013b), and exposure-time integrated limb darkened transit light curves.
- *exoplanet-core*² provides efficient, well-tested, and differentiable implementations of all of the exoplanet-specific operations that must be compiled for performance. These include an efficient solver for Kepler's equation (based on the algorithm proposed by Raposo-Pulido & Peláez, 2017) and limb darkened transit light curves (Agol et al., 2020). Besides the implementation for PyMC3, *exoplanet-core* includes implementations in *numpy* (Harris et al., 2020) and *jax* (Bradbury et al., 2018).
- *celerite2*³, is an updated implementation of the *celerite* algorithm⁴ (Foreman-Mackey, 2018; Foreman-Mackey et al., 2017) for scalable Gaussian Process regression for time series data. Like *exoplanet-core*, *celerite2* includes support for *numpy*, *jax*, and PyMC3, as well as some recent generalizations of the *celerite* algorithm (Gordon et al., 2020).
- *pymc3-ext*⁵, includes a set of helper functions to make PyMC3 more amenable to the typical astronomical data analysis workflow. For example, it provides a tuning schedule for PyMC3's sampler (based on the method used by the Stan project and described by Carpenter et al., 2017) that provides better performance on models with correlated parameters.
- *rebound-pymc3*⁶ provides an interface between *REBOUND* (Rein & Liu, 2012), *REBOUNDx* (Tamayo et al., 2020), and PyMC3 to enable inference with full N-body orbit integration.

¹<https://github.com/exoplanet-dev/exoplanet>

²<https://github.com/exoplanet-dev/exoplanet-core>

³<https://celerite2.readthedocs.io>

⁴<https://celerite.readthedocs.io>

⁵<https://github.com/exoplanet-dev/pymc3-ext>

⁶<https://github.com/exoplanet-dev/rebound-pymc3>

Documentation & case studies

The main documentation page for the *exoplanet* libraries lives at docs.exoplanet.codes where it is hosted on [ReadTheDocs](https://readthedocs.org/). The tutorials included with the documentation are automatically executed on every push or pull request to the GitHub repository, with the goal of ensuring that the tutorials are always compatible with the current version of the code. The *celerite2* project has its own documentation page at celerite2.readthedocs.io, with tutorials that are similarly automatically executed.

Alongside these documentation pages, there is a parallel “Case Studies” website at gallery.exoplanet.codes that includes more detailed example use cases for *exoplanet* and the other libraries described here. Like the tutorials on the documentation page, these case studies are automatically executed using GitHub Actions, but at lower cadence (once a week and when a new release of the *exoplanet* library is made) since the runtime is much longer. [Figure 1](#) shows the results of two example case studies demonstrating some of the potential use cases of the *exoplanet* software ecosystem.

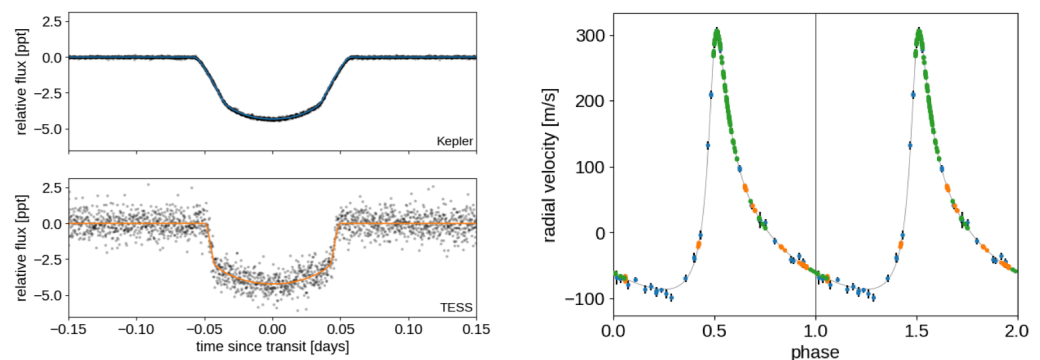


Figure 1: Some examples of datasets fit using *exoplanet*. The full analyses behind these examples are available on the “Case Studies” page as Jupyter notebooks. (left) A fit to the light curves of a transiting exoplanet observed by two different space-based photometric surveys: Kepler and TESS. (right) The phase folded radial velocity time series for an exoplanet observed from different observatories with different instruments, fit simultaneously using *exoplanet*.

Similar tools

There is a rich ecosystem of tooling available for inference with models such as the ones supported by *exoplanet*. Each of these tools has its own set of strengths and limitations and we will not make a detailed comparison here, but it is worth listing some of these tools and situating *exoplanet* in this context.

Some of the most popular tools in this space include (and note that this is far from a comprehensive list!) EXOFAST (J. Eastman et al., 2013; J. D. Eastman et al., 2019), *radvel* (Fulton et al., 2018), *juliet* (Espinoza et al., 2019), *exostriker* (Trifonov, 2019), *PYANETI* (Barragán et al., 2019), *allesfitter* (Günther & Daylan, 2021), and *orbitize* (Blunt et al., 2020). Similar tools also exist for modeling observations of eclipsing binary systems, including *JKTEBOP* (Southworth et al., 2004), *eb* (Irwin et al., 2011), and *PHOEBE* (Conroy et al., 2020). These packages all focus on providing a high-level interface for designing models and then executing a fit. *exoplanet*, however, is designed to be lower level and more conceptually similar to tools like *batman* (Kreidberg, 2015), *PyTransit* (Hannu Parviainen, 2015), *ldtk* (H. Parviainen & Aigrain, 2015), *ellc* (Maxted, 2016), *starry* (Luger et al., 2019), or *Limbdark.jl* (Agol et al., 2020), which provide the building blocks for evaluating the models required for inference with *exoplanet* datasets. In fact, several of the higher-level

packages listed above include these lower-level libraries as dependencies, and our hope is that `exoplanet` could provide the backend for future high-level libraries.

As emphasized in the title of this paper, the main selling point of `exoplanet` when compared to other tools in this space is that it supports differentiation of all components of the model and is designed to integrate seamlessly with the `aesara` (Willard et al., 2021) automatic differentiation framework used by `PyMC3`. It is worth noting that `aesara` was previously known as `Theano` (Theano Development Team, 2016), so these names are sometimes used interchangeably in the `PyMC3` or `exoplanet` documentation⁷. This allows the use of modern inference algorithms such as No U-Turn Sampling (Hoffman & Gelman, 2014) or Automatic Differentiation Variational Inference (Kucukelbir et al., 2017). These algorithms can have some computational and conceptual advantages over inference methods that do not use gradients, especially for high-dimensional models. The computation of gradients is also useful for model optimization; this is necessary when, say, searching for new exoplanets, mapping out degeneracies or multiple modes of a posterior, or estimating uncertainties from a Hessian. Care has been taken to provide gradients which are numerically stable, and more accurate and faster to evaluate than finite-difference gradients.

Acknowledgements

We would like to thank the Astronomical Data Group at Flatiron for listening to every iteration of this project and for providing great feedback every step of the way.

This research was partially conducted during the *Exostar19* program at the *Kavli Institute for Theoretical Physics* at UC Santa Barbara, which was supported in part by the National Science Foundation under Grant No. NSF PHY-1748958.

Besides the software cited above, `exoplanet` is also built on top of `ArviZ` (Kumar et al., 2019) and `AstroPy` (Astropy Collaboration et al., 2018, 2013).

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⁷More information about this distinction is available at <https://docs.exoplanet.codes/en/stable/user/theano/>

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