




ewstools: A Python package for early warning signals of bifurcations in time series data

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Summary

Many systems in nature and society have the capacity to undergo critical transitions: sudden and profound changes in dynamics that are hard to reverse. Examples include the outbreak of disease, the collapse of an ecosystem, and the onset of a cardiac arrhythmia. From a mathematical perspective, these transitions may be understood as the crossing of a bifurcation (tipping point) in an appropriate dynamical system model. In 2009, Scheffer and colleagues proposed early warning signals (EWS) for bifurcations based on statistics of noisy fluctuations in time series data ([Scheffer et al., 2009](#)). This spurred massive interest in the subject, resulting in a multitude of different EWS for anticipating bifurcations ([Clements & Ozgul, 2018](#)). More recently, EWS from deep learning classifiers have outperformed conventional EWS on several model and empirical datasets, whilst also providing information on the type of bifurcation ([Bury et al., 2021](#)). Software packages for EWS can facilitate the development and testing of EWS, whilst also providing the scientific community with tools to rapidly apply EWS to their own data.

ewstools is an accessible Python package for computing, analysing, and visualising EWS in time series data. The package provides:

- An intuitive, object-oriented framework for working with EWS in a given time series
- A suite of temporal EWS and associated methods ([Dakos et al., 2012](#))
- A suite of spectral EWS ([Bury et al., 2020](#))
- Methods to use deep learning classifiers for EWS ([Bury et al., 2021](#))
- Integrated plotting and evaluation functions to quickly check performance of EWS
- Built-in theoretical models to test EWS
- Interactive tutorials in the form of Jupyter notebooks

ewstools makes use of several open-source Python packages, including pandas ([McKinney, 2010](#); [The pandas development team, 2020](#)) for dataframe handling, NumPy ([Harris et al., 2020](#)) for fast numerical computing, Plotly ([Plotly Technologies Inc., 2015](#)) for visualisation, LMFIT ([Newville et al., 2016](#)) for nonlinear least-squares minimisation, ARCH ([Sheppard, 2015](#)) for bootstrapping methods, statsmodels ([Seabold & Perktold, 2010](#)) and SciPy ([Virtanen et al., 2020](#)) for detrending methods, and Keras ([Chollet & others, 2015](#)) and TensorFlow ([Abadi et al., 2016](#)) for deep learning.

Statement of need

Critical transitions are relevant to many disciplines, including ecology, medicine, finance, and epidemiology, to name a few. As such, it is important that EWS are made widely accessible. To my knowledge, there are two other software packages developed for computing EWS, namely [earlywarnings](#) by Dakos et al. (2012) and [spatialwarnings](#) by Génin et al. (2018),

which both use the R programming language. Given the recent surge in popularity of the Python programming language (PYPL, 2022), a Python-based implementation of EWS should be useful. ewstools also implements novel deep learning methods for EWS, which have outperformed conventional EWS in several model and empirical systems (Bury et al., 2021). These new methods should be tried, tested, and developed for a variety of systems and I hope that this package facilitates this endeavour.

Usage Example

```
import ewstools

# Load data and get time series as a pandas Series object
df = pd.read_csv('data.csv')
series = df['x']

# Initialise ewstools TimeSeries object and define transition time
ts = ewstools.TimeSeries(data=series, transition=440)

# Detrend time series
ts.detrend(method='Lowess', span=0.2)

# Compute desired EWS
ts.compute_var(rolling_window=0.5)
ts.compute_auto(lag=1, rolling_window=0.5)
ts.compute_auto(lag=2, rolling_window=0.5)

# Compute performance metrics
ts.compute_ktau()

# Plot results - can be saved as an interactive html file or as a static image
fig = ts.make_plotly()
```

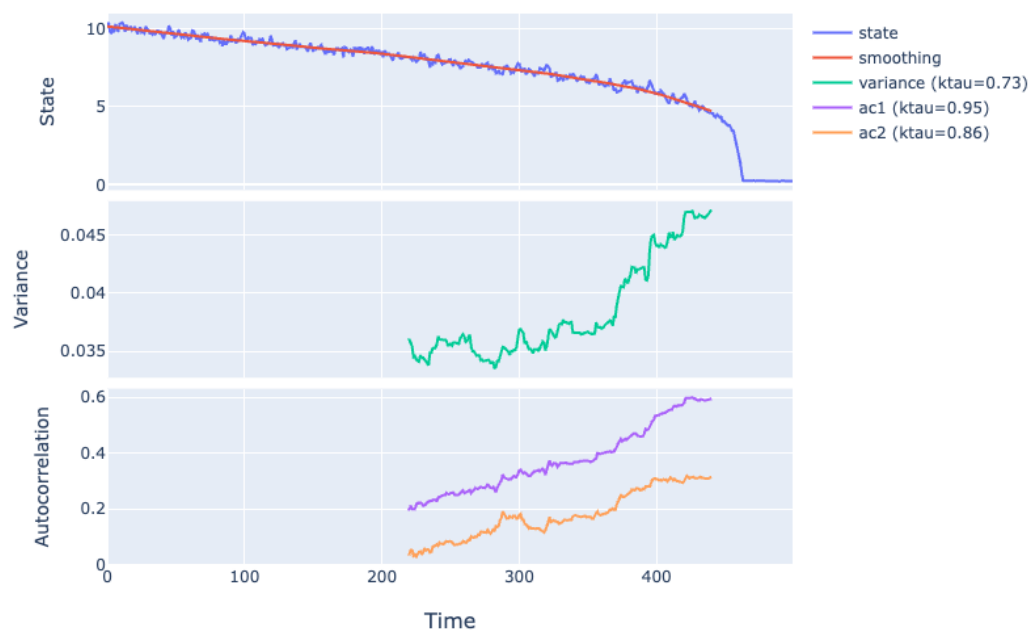


Figure 1: Output of plotting function in usage example.

Documentation

Documentation for ewstools is available at <https://ewstools.readthedocs.io/en/latest/>. Tutorials in the form of Jupyter notebooks are available at <https://github.com/ThomasMBury/ewstools/tree/main/tutorials>.

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