




# Gyselalib++: A Portable C++ Library for Semi-Lagrangian Kinetic and Gyrokinetic Simulations


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## Summary

Gyselalib++ provides the mathematical building blocks to construct kinetic or gyrokinetic plasma simulation codes in C++, simulating a distribution function discretised in phase space on a fixed grid. It relies on the Discrete Domain Computation (DDC) library ([Padioleau et al., 2025](#)) to statically type the discretisation dimensions, thus preventing many common sources of errors. Via DDC, Gyselalib++ also leverages the Kokkos framework ([Trott et al., 2022](#)), ensuring performance portability across various CPU and GPU architectures. The library provides a variety of tools including semi-Lagrangian advection operators, quadrature rules, and solvers for elliptic and hyperbolic partial differential equations (PDEs). The majority of the operators are designed to work on non-orthonormal coordinate systems; those that don't use the static typing to raise compiler errors preventing their misuse.

## Gyrokinetic Simulations

Plasma simulations are essential for the development of magnetic confinement fusion devices for energy production. The low collisionality of such plasmas makes kinetic models a judicious choice. In particular, gyrokinetic theory ([Brizard & Hahm, 2007](#); [Krommes, 2012](#)), which reduces the 6D problem to a 5D problem by removing high-frequency gyromotion, is a popular framework for plasma simulation ([Garbet et al., 2010](#)). Despite the reduction in dimensionality, such simulations still require massively powerful high-performance computing (HPC) resources. For ITER<sup>1</sup>-sized simulations, exascale resources would still be required.

The pre-existing GYSELA code ([Grandgirard et al., 2016](#)), written in Fortran, originally aimed to simulate plasma in the core region of a tokamak using semi-Lagrangian advection with a distribution function discretised in phase space on a uniform grid. This approach was shown to work well, and it allowed the study of many interesting physical phenomena ([Dif-Pradalier et al., 2022](#); [Estève et al., 2018](#); [Sarazin et al., 2021](#)). However, expanding this code to use more complex mathematical methods such as non-uniform points (vital for handling the different magnitudes of physical quantities in the core and edge regions), and increasingly complex geometries (such as D-shape geometries, geometries including both open and closed field lines, X-points, and potentially stellarator geometries) has proved to be challenging and sometimes error-prone. These complexities are further amplified when trying to port such a code to GPU architectures, which are necessary for exascale simulations. This is a challenge shared by other gyrokinetic codes ([Trilaksono et al., 2025](#)).

<sup>1</sup><https://www.iter.org/>

## Statement of Need

In the case of GYSELA, the changes necessary to add non-uniform points and simplify the implementation of other new features, would have required an effort comparable to a complete rewrite, whereas actually performing such a rewrite brings additional benefits for design and portability. For example, we have been able to capitalise on C++'s strengths by using template programming to enforce the correctness of the implemented equations. A common source of error is writing equations with implicit assumptions, such as assuming an orthonormal coordinate system, or specific properties like those of a circular coordinate system. In Gyselalib++, equations are either expressed in tensor notation, so that they are either accurate for all geometries or do not compile, or they explicitly state their dependencies. C++ further enables us to add static assertions for cases with restricted applicability to prevent their misuse. Additionally, DDC is used to encode grid information directly in the type of each field, allowing the compiler to catch indexing errors at compile time. This is particularly useful when working with multiple grids along the same dimension, or when assigning different memory layouts to different fields.

In contrast to GYSELA, Gyselalib++ was conceived of and developed as a library, similar to the SeLaLib Fortran library ([The SeLaLib project team, 2023](#)), whose independent elements are each unit-tested and can be combined to build a final simulation. This design makes the library more versatile, enabling users to rapidly assemble a wide range of simulations, including high-dimensional test cases. The shared elements also provide more confidence in the reliability of the implementation, as they can prove their validity across multiple applications.

## State of the Field

Most established gyrokinetic simulations, such as GENE-X ([Michels et al., 2021](#)) and GT5D ([Idomura et al., 2009](#)), are written in Fortran as stand-alone codes. This limits code sharing and reuse between projects. In contrast, many particle-in-cell codes, such as WarpX ([Vay et al., 2018](#)) and XGC ([Ku et al., 2018](#)), are now developed around reusable libraries like AMReX ([Zhang et al., 2019](#)) and Cabana ([Slattery et al., 2022](#)). To our knowledge, Gyselalib++ is the first such C++ library capable of Eulerian or semi-Lagrangian gyrokinetic applications. The Fortran library SeLaLib ([The SeLaLib project team, 2023](#)) plays a similar role in Fortran.

## Contents

Gyselalib++ includes a range of reusable mathematical operators for plasma simulations. These include, but are not limited to, semi-Lagrangian advection schemes, numerical quadrature, differential operators (e.g. finite difference methods), solvers for common PDEs, and a multi-species collision operator ([Donnel et al., 2019](#)). A complete list of operators is available in the documentation<sup>2</sup>. Many of these tools are designed to work on a variety of grids, including non-uniform grids, which are especially important in edge-region simulations. The library also supports MPI-based parallelism, either with distributed operators or with transpositions between different multi-rank storage layouts.

The VOICE code ([Bourne et al., 2023](#)) has already been rewritten in C++ using the mathematical tools provided by Gyselalib++. Several common simulations including Landau damping (in 2D or in 4D MPI-parallelised Cartesian phase-space coordinates), a bump-on-tail instability (in 2D Cartesian phase-space coordinates), and a guiding-centre model (in polar coordinates) have also been implemented. While these examples are included primarily for illustration, they also serve as valuable testbeds for developing and validating new numerical methods. As such, these examples are ideal for mathematicians looking to validate new methods in realistic, publication-ready test cases.

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<sup>2</sup><https://gyselax.github.io/gyselalibxx/>

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